Date - Morning/Afternoon
GCSE (9-1) MATHEMATICS
J560/06 Paper 6 (Higher Tier)

PRACTICE PAPER (SET 2) MARK SCHEME

Duration: 1 hour 30 minutes

MAXIMUM MARK 100

| DRAFT |
| :---: |

## Subject-Specific Marking Instructions

1. M marks are for using a correct method and are not lost for purely numerical errors.

A marks are for an accurate answer and depend on preceding $\mathbf{M}$ (method) marks. Therefore M0 A1 cannot be awarded.
B marks are independent of $\mathbf{M}$ (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage.
SC marks are for special cases that are worthy of some credit.
2. Unless the answer and marks columns of the mark scheme specify $\mathbf{M}$ and $\mathbf{A}$ marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working full marks should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, i.e. incorrect working is seen and the correct answer clearly follows from it.
3. Where follow through (FT) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word their for clarity, e.g. FT $180 \times$ (their ' $37^{\prime}+16$ ), or FT $300-\sqrt{ }\left(\right.$ their ${ }^{\prime} 5^{2}+7^{2}$ ). Answers to part questions which are being followed through are indicated by e.g. FT $3 \times$ their (a).

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.
4. Where dependent (dep) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.
5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- figs 237, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point e.g. $237000,2.37,2.370,0.00237$ would be acceptable but 23070 or 2374 would not.
- isw means ignore subsequent working after correct answer obtained and applies as a default.
- nfww means not from wrong working.
- oe means or equivalent.
- rot means rounded or truncated.
- seen means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- soi means seen or implied.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (i.e. isw) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.
7. In questions with a final answer line following working space,
(i) if the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation $\checkmark$ next to the correct answer.
(ii) if the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation $\checkmark$ next to the correct answer.
(iii) if the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation $x$ next to the wrong answer.
8. In questions with a final answer line:
(i) If one answer is provided on the answer line, mark the method that leads to that answer.
(ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
(iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
(i) If a single response is provided, mark as usual.
(ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for $\mathbf{A}$ and $\mathbf{B}$ marks. Deduct 1 mark from any $\mathbf{A}$ or $\mathbf{B}$ marks earned and record this by using the MR annotation. M marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75 , which is seen in the working. The candidate then rounds or truncates this to $15.8,15$ or 16 on the answer line. Allow full marks for the 15.75.
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | (a) |  | 1.58 final answer | $\begin{gathered} 2 \\ \text { 1 AOI.2 } \\ 1 \text { AO1.3a } \end{gathered}$ | M1 for 1.57[7...] seen or their answer seen to more than 2dp corrected to 2dp | Both rounded and unrounded value must be seen |
|  | (b) | (i) | $(1+n)^{3}=27^{2}=729$ | $\begin{gathered} 1 \\ 1 \text { AO2. } 2 \end{gathered}$ |  |  |
|  |  | (ii) | 8 | $\begin{gathered} 1 \\ 1 \text { AO3.1a } \end{gathered}$ |  |  |
| 2 | (a) |  | Any two from 1, 2, 3, 4, 6 | $\begin{gathered} 1 \\ 1 \text { AO2.1a } \end{gathered}$ |  |  |
|  | (b) |  | Any valid explanation | $\begin{gathered} 1 \\ 1 \text { AO2.4a } \end{gathered}$ |  | e.g. $\sqrt{S}$ is a factor |
| 3 | (a) |  | Insufficient trials | $\begin{gathered} 1 \\ 1 \text { AO2.5a } \end{gathered}$ |  | Any acceptable reason |
|  | (b) |  | $\begin{aligned} & \hline 11 \\ & 8 \\ & 1 \end{aligned}$ | $\begin{gathered} 3 \\ \begin{array}{c} \text { AOO1.3b } \\ 2 \text { AOO. } 1 \mathrm{bb} \end{array} \end{gathered}$ | B2 for two correct or for one correct with total balls $=20$ Or M1 for $\frac{66}{120} \times 20$ or $\frac{47}{120} \times 20$ or $\frac{7}{120} \times 20$ |  |
| 4 | (a) |  | Final amount is less than initial investment | $\begin{gathered} 1 \\ 1 \text { AO3.4b } \end{gathered}$ |  | Or equivalent correct reason |
|  | (b) |  | Used an incorrect multiplier for the interest rate | $\begin{gathered} 1 \\ 1 \text { AO3.4a } \end{gathered}$ |  | Or equivalent correct reason |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (c) | 6498.40 or 6498.39 | $\begin{gathered} 3 \\ 3 \text { AO1.3a } \end{gathered}$ | $\begin{aligned} & \text { M2 for } 5800 \times 1.023^{5} \\ & \text { Or M1 for } 5800 \times 1.023^{n} \text { oe } \end{aligned}$ | Where $n \geq 1, n \neq 5$ |
| 5 | (a) | $1.6 \text { or } \frac{8}{5} \text { oe }$ | $\begin{gathered} 3 \\ 3 \text { AO1.3b } \end{gathered}$ | M1 for 2(3x-4) $=x$ or $6 x-8=x$ M1FT for $6 x-x=8$ | Alternative method: M2 for $3 x-\frac{x}{2}=4$ Or M1 for $3 x-4-\frac{x}{2}=0$ |
|  | (b) | $x=[ \pm] \sqrt{\frac{y+2}{3}}$ | $\begin{gathered} 3 \\ 3 \text { AO1.3a } \end{gathered}$ | M1 for $y+2=3 x^{2}$ <br> M1FT for $\frac{y+2}{3}=x^{2}$ |  |
| 6 | (a) | 175 | $\begin{gathered} 1 \\ 1 \text { AO1.3a } \end{gathered}$ |  |  |
|  | (b) | 28 to 31 with correct working | $\begin{gathered} \hline 4 \\ 2 \text { AOB.1d } \\ 1 \mathrm{AAOO} .2^{2} \\ 1 \mathrm{AO} 3.3 \end{gathered}$ | M2 for $0.7 \times$ their 175 oe and $0.85 \times$ their 175 oe <br> Or M1 for $0.7 \times$ their 175 oe or $0.85 \times$ their 175 oe <br> AND <br> M1 for reading from graph using their cardio interval | Implied by 122.5 or 123 and 148.75 or 149 seen <br> Using their max and min cardio rates |
|  | (c) | Heart rate out of zone for about 4 minutes | $\begin{gathered} 1 \\ 1 \text { AO2.4a } \end{gathered}$ |  | Or heart rate less than 87.5 during the 50 minutes |
| 7 |  | 69 | $\begin{gathered} 4 \\ 1 \text { AO1.3b } \\ 2 \mathrm{AOH3.1d} \\ 1 \mathrm{AO} 3.3 \end{gathered}$ | M1 for $n-6+n+3 n=109$ oe M1FT for $5 n=109+6$ <br> A1 for $n=23$ | Allow equivalent part marks for use of different person as starting point <br> Rearrangement of their equation to isolate $n$ terms |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8 |  | 604.8 kg | $\begin{gathered} 4 \\ 1 \text { AO1.1 } \\ 1 \text { AO1.3b } \\ \text { 1 AO3.1d } \\ 1 \text { AO3.2 } \end{gathered}$ | B3 for answer 10.08 [kg] OR <br> M1 for $400 \times 400 \times 28$ soi <br> M1 for their volume $\div 1000^{3}$ soi <br> M1 for $2250 \times$ their volume [ $\times 60$ ] soi | Volume calculation using consistent units Conversion of mm to m for all 3 dimensions done at any stage Calculation of mass of 1 or 60 slabs |
| 9 | (a) | $\frac{4}{10}$ oe on first set of branches $\frac{5}{9}, \frac{4}{9}, \frac{6}{9}, \frac{3}{9}$ on second set of branches | $\begin{gathered} 2 \\ 2 \text { AO2.3b } \end{gathered}$ | B1 for two or more correct probabilities |  |
|  | (b) | $\frac{8}{15}$ | $\begin{gathered} \hline 3 \\ 2 \text { AOD.3b } \\ 1 \text { AO2.3a } \end{gathered}$ | M2 for $\frac{6}{10} \times \frac{4}{9}+\frac{4}{10} \times \frac{6}{9}$ oe Or M1 for $\frac{6}{10} \times \frac{4}{9}$ oe or $\frac{4}{10} \times \frac{6}{9}$ oe | FT probabilities from their tree diagram for method marks |
| 10 | (a) | $\begin{aligned} & 3.20 \times 10^{6} \\ & 4.04 \times 10^{5} \end{aligned}$ | $\begin{gathered} 2 \\ 1 \text { AO1.2 } \\ 1 \text { AO2.3b } \end{gathered}$ | B1 for one correct or for $3.195[3] \times 10^{6}$ and $4.042 \times 10^{5}$ or for $3.20 \times 10^{m}$ and $4.04 \times 10^{n}$ | Where $m$ and $n$ are integers |
|  | (b) | $3.54 \times 10^{7}$ | $\begin{gathered} 1 \\ 1 \text { A01.3a } \end{gathered}$ |  |  |
|  | (c) | $5.7[0] \times 10^{5}$ | $\begin{gathered} 3 \\ \begin{array}{c} 2 \text { AO1.3b } \\ 1 \text { AOO2.3a } \end{array} \end{gathered}$ | B1 for $2.455 \times 10^{6}$ or $1.885 \times 10^{6}$ seen M1 for their $(2.455-1.885) \times 10^{6}$ | Using values in ranges $2.445 \leq n \leq$ 2.455 and $1.885 \leq n \leq 1.895$ |
| 11 | (a) | $\begin{aligned} & \mathrm{E} \\ & \mathrm{~F} \end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { B1 } \\ \text { 2 A02.3a } \end{gathered}$ |  |  |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) |  | $\stackrel{1}{1 \text { AO2.3b }}$ |  | Clear intention |
| 12 | (a) | $24 \quad 48 \quad 71$ | $\begin{gathered} 1 \\ 1 \text { AO2.3b } \end{gathered}$ |  |  |
|  | (b) |  | $\begin{gathered} 2 \\ 2 \text { AO2.3b } \end{gathered}$ | B1FT for at least 5 points plotted correctly If $\mathbf{0}$ scored, SC1 for translation of correct curve |  |
|  | (c) | States correct with comparison showing approximately 18 employees over 55 and one quarter of $80=20$ | $\begin{gathered} 2 \\ 1 \text { AO2.1b } \\ 1 \text { AO2.5a } \end{gathered}$ | FT reading from their cumulative frequency curve at 55 <br> B1 for one quarter of employees $=20$ or for approximately 18 employees over 55 FT their curve |  |
| 13 |  | AM = MD given <br> $\angle \mathrm{BMA}=\angle \mathrm{CMD}$ vertically opposite <br> $\angle \mathrm{BAM}=\angle \mathrm{CDM}$ alternate angles <br> Triangles AMB, DMC congruent, ASA | M1 M1 M1 A1 4 A02.4b | After M0, B2 for two pairs of equal angles and one pair of equal sides with insufficient or no reasons Or B1 for two pairs of equal angles identified | Accept any correct proof |


| Question |  |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14 | (a) |  | $x \leq-3, x \geq 4$ | $\stackrel{3}{3 \text { AO1.3b }}$ | M1 for $(x-4)(x+3)$ <br> A1 for solutions -3 and 4 seen |  |
|  | (b) |  | -2 | $\begin{gathered} 4 \\ 2 \text { AO2.1a } \\ 2 \text { AOB.1b } \end{gathered}$ | M1 for $2 y=x+4$ drawn M1 for $x+y=5$ drawn M1FT for correct region/points identified on graph |  |
| 15 | (a) |  | $\frac{x^{6}}{y^{3}}$ | $\frac{2}{2 \text { A01.3a }}$ | M1 for $\left(\frac{x^{2}}{y}\right)^{3}$ or $\frac{x^{12} y^{3}}{x^{6} y^{6}}$ |  |
|  | (b) | (i) | $\frac{2 x}{y}$ | $\begin{gathered} 1 \\ 1 \text { A01.3a } \end{gathered}$ |  |  |
|  |  | (ii) | $\begin{aligned} & \frac{3 x^{2}+14 x}{(x-2)(x+3)} \text { or } \frac{x(3 x+14)}{(x-2)(x+3)} \\ & \text { or } \frac{x(3 x+14)}{x^{2}+x-6} \end{aligned}$ | $\begin{gathered} 3 \\ 3 \text { A01.3b } \end{gathered}$ | M1 for numerator $4 x(x+3)-x(x-2)$ oe M1 for denominator $(x-2)(x+3)$ oe |  |
| 16 | (a) |  | 1.44 | $\stackrel{3}{3 \text { A01.3a }}$ | M2 for $9 \times 4^{2}=y \times 10^{2} \mathbf{o e}$ Or M1 for $9 \times 4^{2}$ or $y=\frac{k}{x^{2}}$ soi |  |
|  | (b) |  | 56.25 | $\begin{gathered} \hline 3 \\ 1 \text { AO1.3a } \\ 1 \text { AOO.1a } \\ 1 \text { AO3.3 } \end{gathered}$ | M2 for 1.5625 or $\frac{1}{0.8^{2}}$ soi Or M1 for $0.8^{2}$ soi | Alternative method: <br> M1 for calculation of values of $y$ for their $x$ and their $0.8 x$ <br> M1 for calculation of percentage increase in $y$ values |


| Question |  | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 17 | (a) | Gradient $\mathrm{AB}=\frac{4-2}{7-3}=\frac{1}{2}$ <br> Gradient $B C=\frac{-2-4}{10-7}=-2$ <br> Product of gradients $=\frac{1}{2} \times-2=-1$ <br> Perpendicular because product of gradients is -1 | M1 <br> A1 <br> B1 2 AO2.4b 2 A03.1b | Calculation of gradient of $A B$ <br> Calculation of gradient of BC |  |
|  | (b) | $8.06[2 \ldots]$ or $\sqrt{65}$ | $\begin{gathered} 4 \\ \begin{array}{c} \text { A AO1.3b } \\ 1 \text { AOB.1a } \\ 1 \text { AOB.2 } \end{array} \end{gathered}$ | B1 for identifying AC as hypotenuse M2 for $\sqrt{(10-3)^{2}+(2--2)^{2}}$ <br> Or M1 for attempt to use Pythagoras |  |
| 18 | (a) | 3 hours 12 minutes | 6 <br> 2 AO1.3b <br> 2 AO3.1d <br> 1 AOB.2 <br> 1 AOB.3 | $\begin{aligned} & \text { M2 for }\left[\mathrm{AC}^{2}\right] \\ & =2.8^{2}+6.2^{2}-2 \times 2.8 \times 6.2 \times \cos 95 \end{aligned}$ <br> Or M1 for attempt to use cosine rule AND <br> A1 for [AC =] 7.02 <br> M2 for ( $2.8+6.2+$ their 7.02 ) $\div 5$ <br> Or M1 for attempt at their distance $\div 5$ |  |
|  | (b) | Any sensible assumption about distance, speed or time <br> Any sensible explanation | $\begin{gathered} 1 \\ 2 \text { AO3.5 } \end{gathered}$ |  | e.g. he walks in a straight line e.g. he doesn't have a rest <br> e.g. underestimate so time would be longer |
| 19 | (a) | $4 a-3 b$ | $\begin{gathered} 2 \\ 1 \text { AO1.3b } \\ 1 \text { AO2.3b } \end{gathered}$ | B1 for $\overrightarrow{A D}=3 \mathbf{a}$ or $\overrightarrow{B C}=\mathbf{2 b}$ soi | Allow $\overrightarrow{O D}=4 \mathbf{a}$ or $\overrightarrow{O C}=3 \mathbf{b}$ for B1 |


| Question | Answer | Marks | Part marks and guidance |  |
| :---: | :---: | :---: | :---: | :---: |
| (b) | $\begin{aligned} & \overrightarrow{A D}=\overrightarrow{C E}=3 \mathbf{a} \\ & \overrightarrow{A C}=\overrightarrow{D E}=3 \mathbf{b}-\mathbf{a} \end{aligned}$ <br> Opposite sides equal and parallel hence ACED is a parallelogram | $\begin{array}{\|c\|} \hline \text { M2 } \\ \\ \text { M2 } \\ \\ \text { A1 } \\ \text { 1 AO2.4a } \\ \text { 3 AOO.110 } \\ 1 \text { AOB.3 } \end{array}$ | M1 for $\overrightarrow{A D}=3 \mathbf{a}$ or $\overrightarrow{C E}=3 \mathbf{a}$ <br> $\mathbf{M 1}$ for $\overrightarrow{A C}=\mathbf{3 b}-\mathbf{a}$ or $\overrightarrow{D E}=\mathbf{3} \mathbf{b} \mathbf{- a}$ |  |

Assessment Objectives (AO) Grid

| Question | A01 | AO2 | AO3 | Total |
| :---: | :---: | :---: | :---: | :---: |
| 1(a) | 2 | 0 | 0 | 2 |
| 1(b)(i) | 0 | 1 | 0 | 1 |
| 1(b)(ii) | 0 | 0 | 1 | 1 |
| 2(a) | 0 | 1 | 0 | 1 |
| 2(b) | 0 | 1 | 0 | 1 |
| 3(a) | 0 | 1 | 0 | 1 |
| 3(b) | 1 | 2 | 0 | 3 |
| 4(a) | 0 | 0 | 1 | 1 |
| 4(b) | 0 | 0 | 1 | 1 |
| 4(c) | 3 | 0 | 0 | 3 |
| 5(a) | 3 | 0 | 0 | 3 |
| 5(b) | 3 | 0 | 0 | 3 |
| 6(a) | 1 | 0 | 0 | 1 |
| 6(b) | 0 | 0 | 4 | 4 |
| 6(c) | 0 | 1 | 0 | 1 |
| 7 | 1 | 0 | 3 | 4 |
| 8 | 2 | 0 | 2 | 4 |
| 9(a) | 0 | 2 | 0 | 2 |
| 9(b) | 2 | 1 | 0 | 3 |
| 10(a) | 1 | 1 | 0 | 2 |
| 10(b) | 1 | 0 | 0 | 1 |
| 10(c) | 2 | 1 | 0 | 3 |
| 11(a) | 0 | 2 | 0 | 2 |
| 11(b) | 0 | 1 | 0 | 1 |
| 12(a) | 0 | 1 | 0 | 1 |
| 12(b) | 0 | 2 | 0 | 2 |
| 12(c) | 0 | 2 | 0 | 2 |
| 13 | 0 | 4 | 0 | 4 |
| 14(a) | 3 | 0 | 0 | 3 |
| 14(b) | 0 | 2 | 2 | 4 |
| 15(a) | 2 | 0 | 0 | 2 |
| 15(b)(i) | 1 | 0 | 0 | 1 |
| 15(b)(ii) | 3 | 0 | 0 | 3 |
| 16(a) | 3 | 0 | 0 | 3 |
| 16(b) | 1 | 0 | 2 | 3 |
| 17(a) | 0 | 2 | 2 | 4 |
| 17(b) | 2 | 0 | 2 | 4 |
| 18(a) | 2 | 0 | 4 | 6 |
| 18(b) | 0 | 0 | 2 | 2 |
| 19(a) | 1 | 1 | 0 | 2 |
| 19(b) | 0 | 1 | 4 | 5 |
| Totals | 40 | 30 | 30 | 100 |

