## Further Maths GCSE Differentiation Answers

$1 - x^2 + 2x + 1$
1. $y = x^2 + 3x + 4$ $\frac{\partial y}{\partial x} \cdot 2x + 3$
At the Stationary point of =0
so 20+3=0 ⇒ x=-3/2=-1.5
$y = x^2 + 3x + 4 \Rightarrow y = \frac{9}{4} - \frac{9}{4} + 4 = 1.75$
50 Coodinates ar (-1.5, 1.75)
2. $y = (x+1)(2-x) = -x^2 + x + 2$ . So $A = (0,2)$
Dy = -2x+1 so gradicit of target at A
$\Rightarrow x = 0 \Rightarrow \frac{\partial y}{\partial x} = 1$ The gradiest of the normal = $\frac{-1}{1} = -1$
y = mx + c with $m = -1$ and passes through $(0,2)so \lambda = -1 \times 0 + c \Rightarrow c = 2so y = -1x + 2$
A fixed or which Te= x <= 0 = h & control or by the thing or which is both by
$\left\{Attenationary gradient of AP = \frac{4^2-4^2}{x^2-x^2} = \frac{0-2}{2-0} = -1\right\}$

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3 y=px3-3x2+8x+1
   3x = 3x2p -6x+8
 (i) be know that when x=2, y=10
 (ii) Loe also know that when x=2; ox =0
(i) 50 10 = p \times 2^3 - 3 \times 2^4 + 8 \times 2 + 7

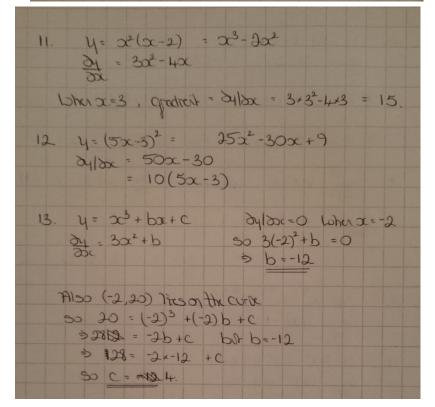
\Rightarrow 10 = 8p - 12 + 16 + 7

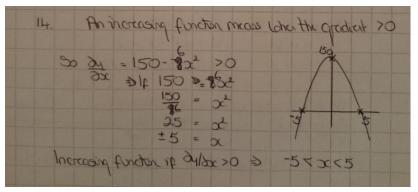
\Rightarrow 6 = 8p + 7
(ii)
 Also \frac{3}{3} = 0 \Rightarrow 3 + 2^2 p - 6 + 2 + 8 = 0
12p + -4 = 0
p = \frac{1}{3}
    Asp=1/3 6=8x1/3+7
 4. y = \frac{3x(3x^4-5x)}{x^2} = \frac{6x^5-15x^2}{x^2} = 6x^3-15
    So 34 = 18022
 5. y = (3x-4)(x+2) + 3x^2+2x-8
  δy: 6x+2 ioherx=2 δy: 14
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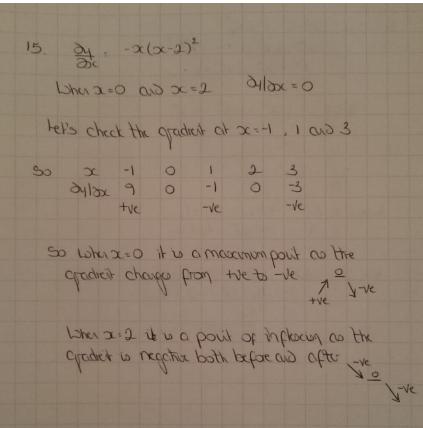
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6. 4= 10-8x-x3
    \frac{34}{37} = -8 - 3x^2 = -(8 + 3x^2)
   2>0 for all Dalou of x > -(8+3x2) <0 (4x)
   >> I is a decreasing function to all x (Ax)
7. Dy = 202-7 Laherox = 3 Dx = 2-(-3)2-7 = 11.
   ox = 1 => 2x²-7=1

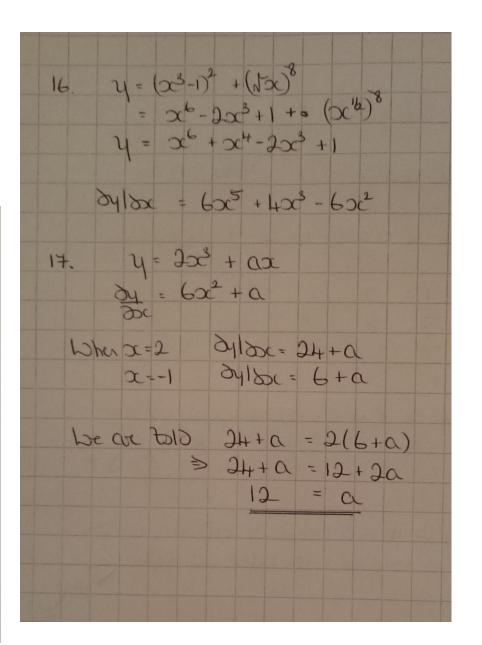
>> 2x²-8
           \Rightarrow x^2 = +1 \quad \Rightarrow x = +1 \quad \Rightarrow -1.
8. y = x^{1/2}(x^{+/2} - x^{-1/2}) = x^{+/2} - x
 À = H33 −1
9, y=4x3+6x2+3xx+5
    ay = 1202 + 120x +3
     dy/2 = 0 => 12x2+12x+3=0
           ( = 3) Hat + Ha + 1 = 0
              \Rightarrow (2x+1)(2x+1) = 0
              => 2x+1=0 sox=-1/2
     as it is a cobic with a sight Statoray poil . inflexion
    34 = 12x tolax + 2 >0 so minimum
    [cools check gradient at -1 and 0 both are +ve]
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10. $P = (3,0)$ Q = (3,0) $y = \infty^2 - 5\infty + 6$	
dy . 20-5	
When x=2 gradient = 24/2x = -1  x=3 " " = 1	
As 1x-1 = -1 the two targets capapadiche	V.









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